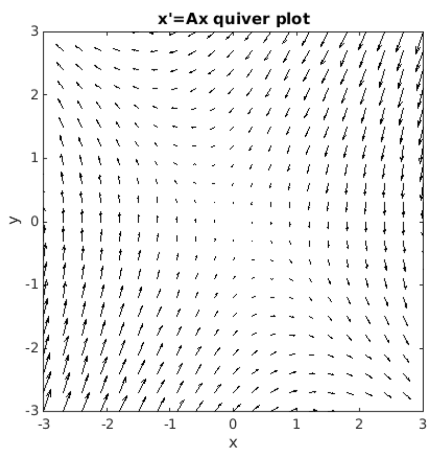
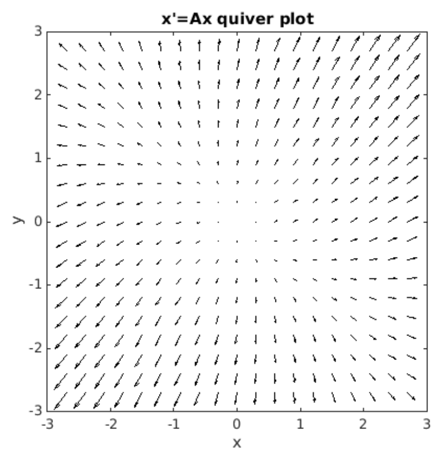
Problems 1-6. The following plots show arrows $\mathbf{x}' = d\mathbf{x}/dt$ for linear systems. $\mathbf{x}' = A\mathbf{x}$. In each case, A has distinct eigenvalues and two eigenvectors.

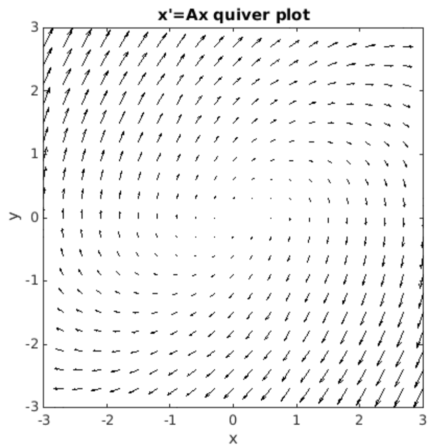
- Say whether the eigenvalues are real or complex.
- If the eigenvalues are real, draw the eigenvectors, label them $\mathbf{v}_1$ and $\mathbf{v}_2$, and specify the signs of λ_1 and λ_2 (e.g Re $\lambda_1 < 0$, Re $\lambda_2 > 0$).
- If the eigenvalues are complex, specify the sign of their real part (e.g Re $\lambda < 0$).
- Draw trajectories starting from the points $(x, y) = (2, 0), (0, 2), (-2, 0)$, and $(0, -2)$.
- If $\mathbf{x}(t) \to 0$ for all choices of initial conditions, then the system $\mathbf{x}' = A\mathbf{x}$ is said to be *stable*. If $\mathbf{x}(t) \to \infty$ for all but very special choices of initial conditions (such as $\mathbf{x}(0)$ lying exactly on an eigenvector), then the system is said tp be *unstable*. Specify whether the system is stable or unstable.

(1)

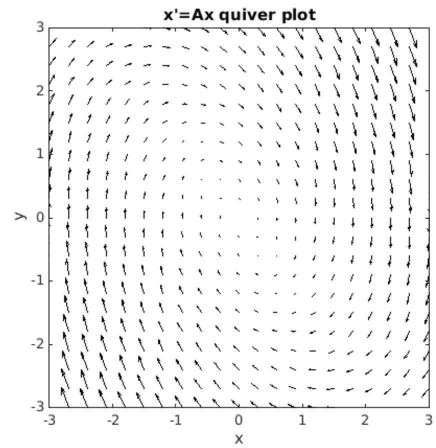


(2)




x'=Ax quiver plot
y
x

(3)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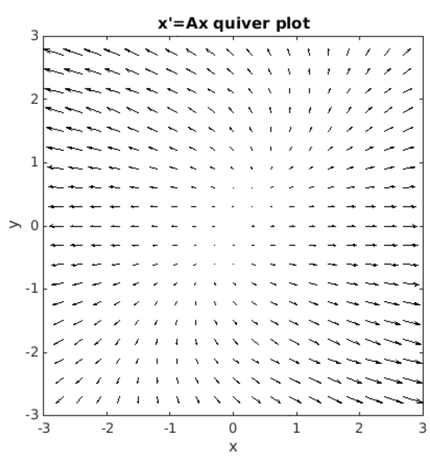
y
x

(4)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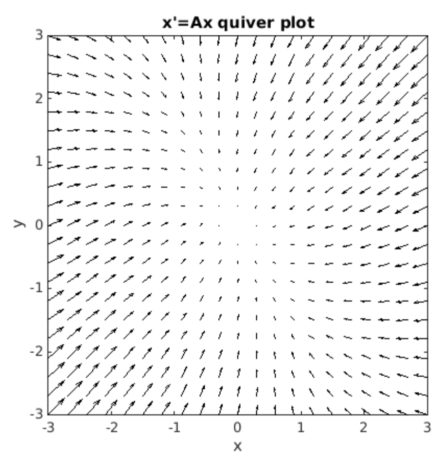
y
x

(5)


x'=Ax quiver plot
y
x

(6)