Homework #11

Math 527, UNH spring 2015

Due Thursday, April 30 in recitation.

For problems with complex eigenvalues, express your answer in both complex and real-valued form.

Problems 1-5. Find the general solution of the system of equations. Prime notation means differentiation in t, i.e. x' = dx/dt. Several of these problems feature eigenvalue problems from problems 7-11 of HW 10.

$$1. \quad x' = -x + 2y$$

$$y' = -7x + 8y$$

2.
$$x' = 2x + 2y$$

$$y' = x + 3y$$

3.
$$x' = -x + 2y$$

$$y' = -5x + y$$

4.
$$x' = 4x + 5y$$

$$y' = -2x + 6y$$

5.
$$x' = -8x - y$$

$$y' = 16x$$

Problem 6. Solve the initial value problem.

$$x' = x/2$$

$$y' = x + y/2$$

$$x(0) = 3, \ y(0) = 5.$$

Problem 7. Find the general solution.

$$x' = 2x + 4y + 4z$$

$$y' = -x - 2y$$

$$z' = -x - 2z$$

Most problems adapted from Section 8.2 and Appendix II of Zill's "First Course in Differential Equations," 9th edition.