INSTRUCTIONS: PLEASE READ CAREFULLY

- 1. Write your name and section number above. 5 pts will deducted if either is missing or illegible.
- 2. Show your work and put a box or circle around your answers.
- 3. Always write equations.
- 4. Partial credit will be given only if your work is written clearly and in equations.

Problem 1. (30 pts) Find the general solution of the differential equation. Solve for y(x) explicitly.

$$\frac{dy}{dx} = -x^2 y^3$$

Problem 2. (30 pts) Find the general solution of the differential equation and then find the solution of the initial value problem. Solve for y(t) explicitly.

$$\frac{dy}{dt} = te^{-t^2} - 2ty, \quad y(0) = 1$$

Problem 3. (30 pts) Find the general solution of the differential equation. An implicit solution is fine.

$$2(y^{2} - e^{-x}\sin 2y)\frac{dy}{dx} = e^{-x}\cos 2y$$

Problem 4: (10 pts) Fill in this chart of substitution methods for 1st order differential equations.

type	general form	substitution	resultant ODE type