Instructions: Differential equations require a good knowledge of calculus. You should be able to do these problems easily and with confidence. Problems $1-21$ are especially simple -you should be able to do them in your head. The other problems will require more work -integration by parts in a few cases. Provide your work for these on attached sheets. One problem cannot be further simplified, the only decent answer is " $X=X$ ", where " $X=$ " is the original problem statement. And remember: Always Write Equations!

1. $\frac{d}{d x} 6 x^{3}=$
2. $\frac{d}{d x} 2 x^{-1}=$
3. $\frac{d}{d x} a x^{n}=$
4. $\frac{d}{d x} \sum_{n=0}^{N} a_{n} x^{n}=$
5. $\frac{d}{d t}(a \cos \omega t+b \sin \omega t)=$
6. $\frac{d}{d x} e^{\alpha x}=$
7. $\frac{d}{d x} \ln \mu x=$
8. $\frac{d}{d x} \sin \alpha x^{2}=$
9. $\frac{d}{d x} x^{2} \sin \alpha x=$
10. $\frac{d}{d x} \frac{x^{2}}{\sin \alpha x}=$
11. $\frac{d}{d x} \sum_{n=0}^{\infty} \frac{1}{n!} \lambda^{n} x^{n}=$
12. $\frac{d}{d x} \int f(x) d x=$
13. $\frac{d}{d x} \int_{0}^{x} f(s) d s=$
14. $\int 8 x^{3} d x=$
15. $\int_{0}^{1} 8 x^{3} d x=$
16. $\int_{0}^{y} 8 x^{3} d x=$
17. $\int \sum_{n=0}^{N} a_{n} x^{n} d x=$
18. $\int \frac{1}{x} d x=$
19. $\int \frac{d}{d x} f(x) d x=$
20. $\int \frac{d y}{d x} d x=$
21. $\int \frac{d^{n} y}{d x^{n}} d x=$
22. $\int y d x=$
23. $\int \ln x d x=$
24. $\int \tan ^{-1} x d x=$
25. $\int \sum_{n=0}^{\infty} \frac{1}{n!} \lambda^{n} x^{n} d x=$
26. Solve the system $3 x^{2}-2 y=0,4 x+y=1$ for $x$ and $y$.

Some Greek letters and their typical use in mathematics.

| $\alpha$ | alpha | real-valued constant |
| :--- | :--- | :--- |
| $\beta$ | beta | real-valued constant |
| $\gamma$ | gamma | real-valued constant |
| $\epsilon$ | epsilon | infinitesimal or very small constant |
| $\lambda$ | lambda | eigenvalue or coefficient in an exponent |
| $\theta$ | theta | an angle |
| $\mu$ | mu | parameter or coefficient in an exponent |
| $\nu$ | nu | parameter |
| $\xi$ | xi | space-like variable, pronounced "cksee" |
| $\sigma$ | sigma | time-like variable |
| $\tau$ | tau | time-like variable |
| $\phi$ | phi | function |
| $\psi$ | psi | function |
| $\omega$ | omega | frequency, i.e. coefficient of $t$ in $\cos \omega t$ |

