Instructions: Differential equations require a good knowledge of calculus. You should be able to do these problems easily. Problems 1-10 and 14-21 are especially simple. You should be able to do these in your head. If you can't, go back to your calculus textbook, study the relevant topic, and work through similar examples until you can. The other problems will require more work -integration by parts in a few cases. Provide your work for these on attached sheets. One problem cannot be further simplifed: the only decent answer is " $\mathrm{X}=\mathrm{X}$ ", where " $\mathrm{X}=$ " is the original problem statement. And remember, AWE: Always Write Equations!

1. $\frac{d}{d x} 6 x^{3}=$
2. $\frac{d}{d x} 2 x^{-1}=$
3. $\frac{d}{d x} a x^{n}=$
4. $\frac{d}{d x} \sum_{n=0}^{N} a_{n} x^{n}=$
5. $\frac{d}{d t}(a \cos \omega t+b \sin \omega t)=$
6. $\frac{d}{d x} e^{\alpha x}=$
7. $\frac{d}{d x} \ln \mu x=$
8. $\frac{d}{d x} \sin \alpha x^{2}=$
9. $\frac{d}{d x} x^{2} \sin \alpha x=$
10. $\frac{d}{d x} \frac{x^{2}}{\sin \alpha x}=$
11. $\frac{d}{d x} \sum_{n=0}^{\infty} \frac{1}{n!} \lambda^{n} x^{n}=$
12. $\frac{d}{d x} \int f(x) d x=$
13. $\frac{d}{d x} \int_{0}^{x} f(s) d s=$
14. $\int 8 x^{3} d x=$
15. $\int_{0}^{1} 8 x^{3} d x=$
16. $\int_{0}^{y} 8 x^{3} d x=$
17. $\int \sum_{n=0}^{N} a_{n} x^{n} d x=$
18. $\int \frac{1}{x} d x=$
19. $\int \frac{d}{d x} f(x) d x=$
20. $\int \frac{d y}{d x} d x=$
21. $\int \frac{d^{n} y}{d x^{n}} d x=$
22. $\int y d x=$
23. $\int \ln x d x=$
24. $\int \tan ^{-1} x d x=$
25. $\int \sum_{n=0}^{\infty} \frac{1}{n!} \lambda^{n} x^{n} d x=$
26. Solve the system $3 x^{2}-2 y=0,4 x+y=1$ for $x$ and $y$.

Some Greek letters you should know and their typical mathematical use

| $\alpha$ | alpha | real-valued constant |
| :--- | :--- | :--- |
| $\beta$ | beta | real-valued constant |
| $\gamma$ | gamma | real-valued constant |
| $\epsilon$ | epsilon | infinitesimal or very small constant |
| $\lambda$ | lambda | eigenvalue or coefficient in an exponent |
| $\theta$ | theta | an angle |
| $\mu$ | mu | parameter or a coefficient in an exponent |
| $\nu$ | nu | a parameter |
| $\xi$ | xi | pronounced "cksee" |
| $\rho$ | rho |  |
| $\sigma$ | tau | time-like variable |
| $\phi$ | phi | function |
| $\psi$ | psi | function |
| $\omega$ | omega | frequency, i.e. coefficient of $t$ in $\cos \omega t$ |

